# Neutron stars spectra Probing the equation of state of dense matter

# Frédéric Vincent<sup>1</sup>, M. Bejger, A. Różańska, O. Straub, T. Paumard, M. Fortin, J. Madej, B. Beldycki

<sup>1</sup>CNRS/Observatoire de Paris/LESIA





Credit : T. Piro

- Accretion  $\rightarrow$  H, He atmosphere
- He runaway burning: burst
- Full star's surface shining Xrays
- Goal: model this; compare to obs

#### Interest of NS spectra

• Flux: 
$$F_{\infty} = \sigma \left(\frac{R_{\infty}}{D}\right)^2 T_{\infty}^4$$
; Observed:  $F_{\infty}, T_{\infty}$ 

- Light bending (Schwarzschild):  $R_{\infty} = R_{\star} \left(1 \frac{2M_{\star}}{R_{\star}}\right)^{-1/2}$
- Observed spectrum  $\rightarrow$  constraint on  $M_{\star}, R_{\star}$
- Interest: constrain EoS

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Credit: M. Fortin

Neutron stars spectra

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# State of the art for fitting NS spectra

- Ray trace photons to distant observer
- Emission: pure blackbody
- **Spacetime**: Schwarzschild, Kerr, Hartle-Thorne (analytic approx)
- Star rotation: often neglected, or small

(some recent analyses go further: Cadeau+, Baubock+)

### Our goal

- More realistic emission  $I_{\nu}(\tau, \cos i)$
- Accurate spacetime (numerical)
- Valid for any rotation

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#### Lorene metric

- Input: *M*<sub>\*</sub>, Ω<sub>\*</sub>, EoS
- Solves Einstein equation
- Output: *g*<sub>μν</sub>, **u**<sub>\*</sub>

# ATM21 atmosphere

- Input: atm composition,  $T_{\rm eff}, g_{\rm surf}(g_{\mu\nu})$
- Solves hydrostatic and radiative equilibria, emissivity: blackbody+Compton; absorption: free-free
- Output: Emergent intensity, function of local angle

# Gyoto raytracing

- Input: the 2 previous outputs
- Transports the radiation in the metric
- Output: observed spectrum

# Setup chosen

- NS with EoS SLy4 (Douchin&Haensel01, Chabanat+98)
- $M_{\star} = 1.4 \, M_{\odot}, \, \Omega_{\star} = 0;716 \; \text{Hz}$
- Atm: H+He, solar abundance,  $T_{\rm eff} = 10^7$  K

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### Local spectra



### What impacts emitted intensity



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# Ray-traced images, face-on



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## Ray-traced images, edge-on fast-rotating



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# Ray-traced images, $(\Omega, i)$



Frédéric Vincent Neutron stars spectra



At high energy, Doppler + steep spectrum = strong beaming so rotating case very different wrt the non-rotating case.

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For rotating star, beaming varies like observed energy

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