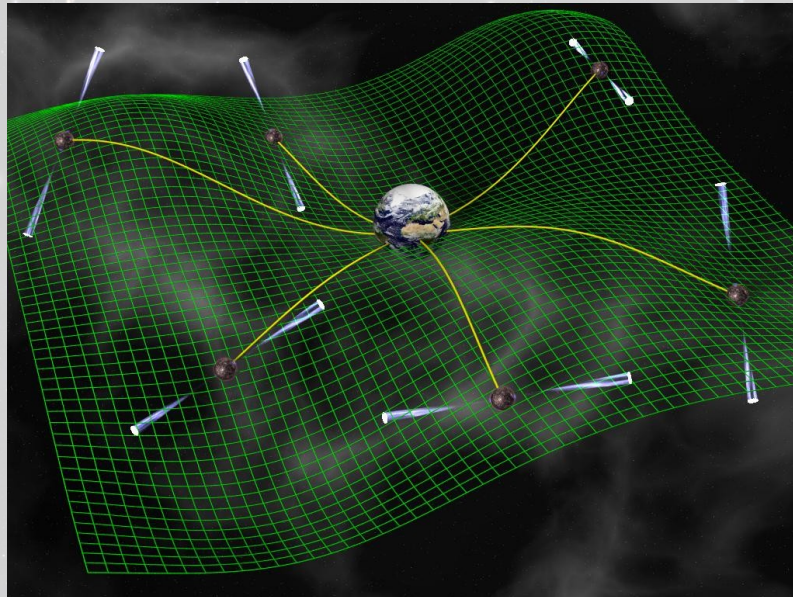
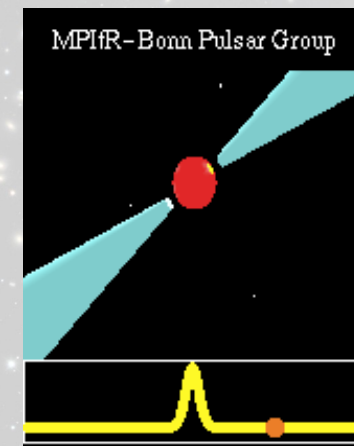
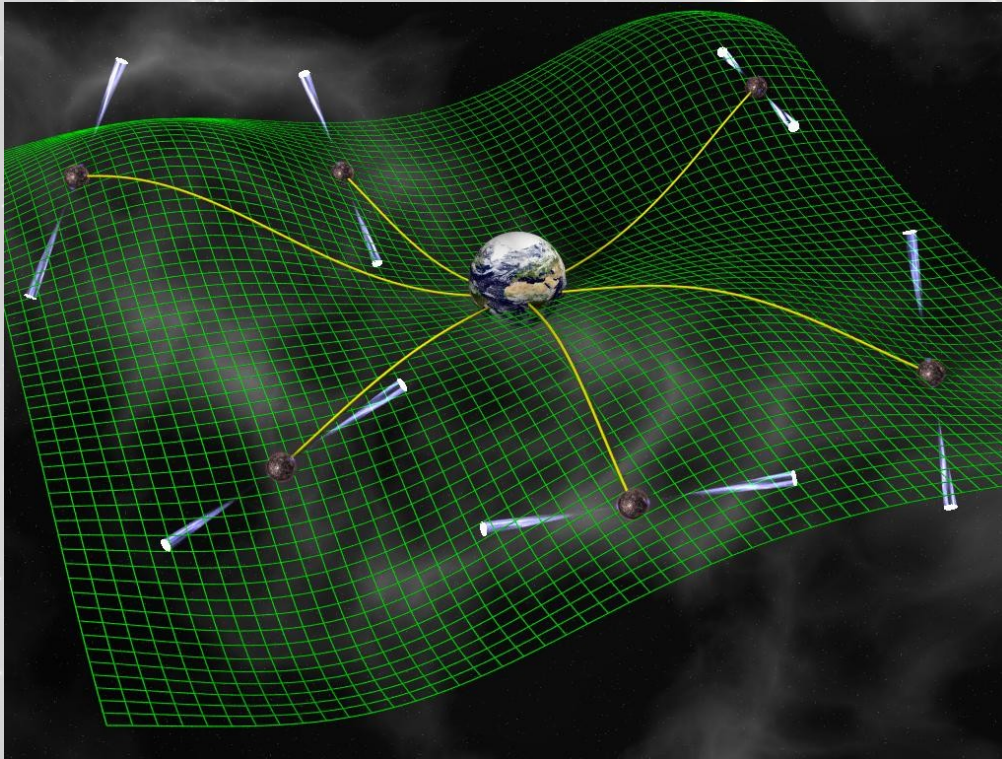


Pulsar Timing Arrays

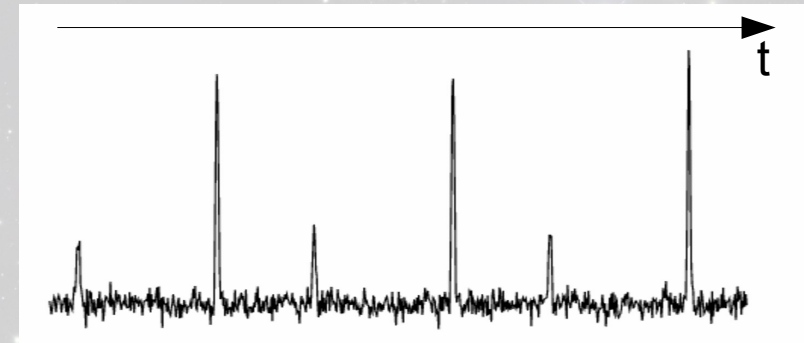


Gphys, May 2014, Observatoire de Paris
G.Theureau

Pulsar Timing Arrays : principles



Millisecond pulsars
Considered as quasi perfect clocks



Earth and distant PSR treated as free masses
whose positions respond to changes in the local space time metric

→ *A passing GW perturbs the metric
and produces fluctuations in the measured TOAs*

If uncertainty dt and length of data span T

→ *sensitive to amplitude dt/T and frequencies $f \sim 1/T$*

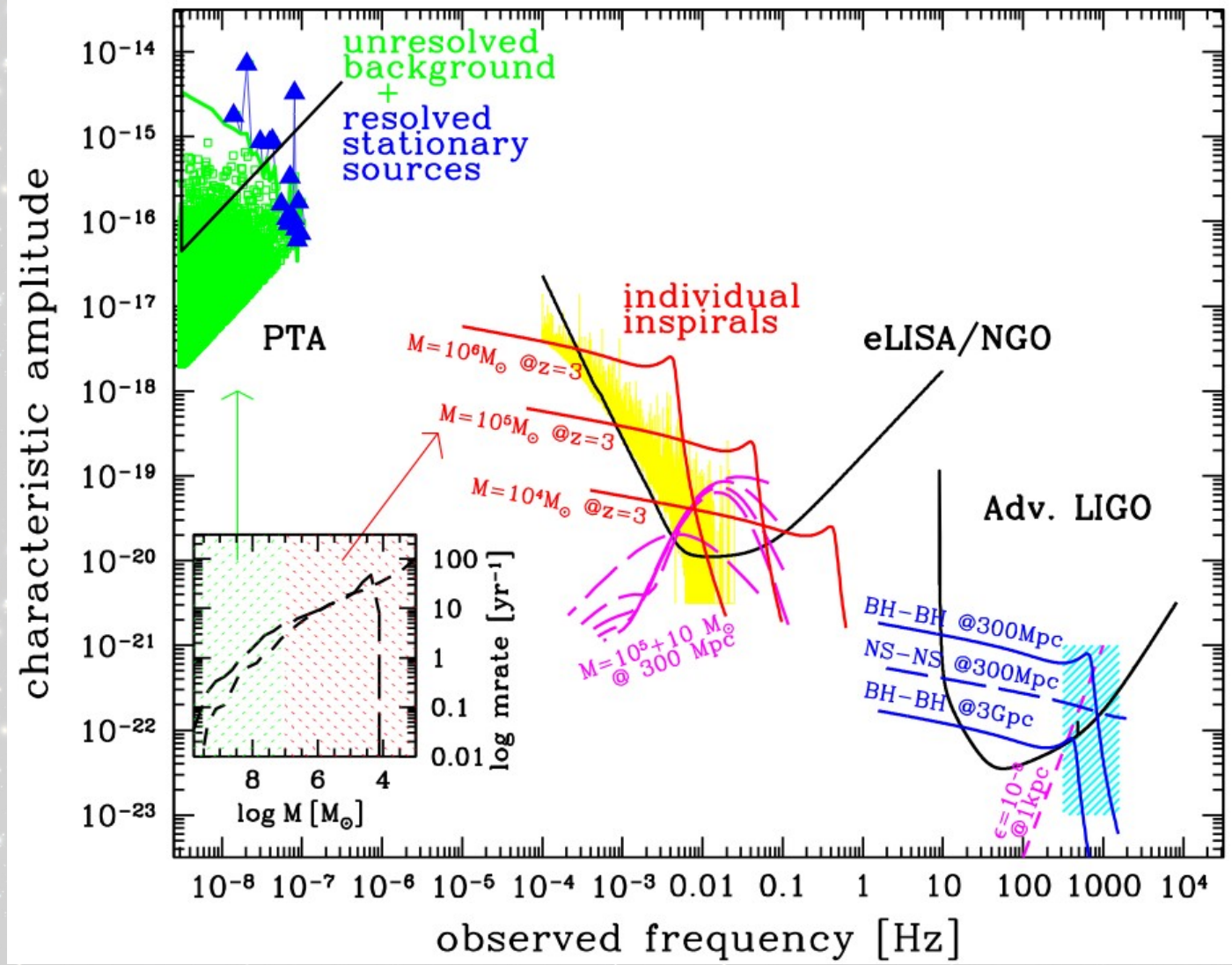
Frequency domain → $10^{-9} - 10^{-7}$ Hz

Gravitational waves background :

The nanoHertz regime

- Super massive binary black holes
- Cosmic string loops
- Relics of inflation

$$h_c(f) = A \left(\frac{f}{\text{yr}^{-1}} \right)^\alpha$$



Model	A	α	References
Supermassive black holes	$10^{-15} - 10^{-14}$	$-2/3$	Jaffe & Backer (2003) Wyithe & Loeb (2003) Enoki et al. (2004)
Relic GWs	$10^{-17} - 10^{-15}$	$-1 - -0.8$	Grishchuk (2005)
Cosmic String	$10^{-16} - 10^{-14}$	$-7/6$	Maggiore (2000)

Super Massive Binary Black Holes

Population models

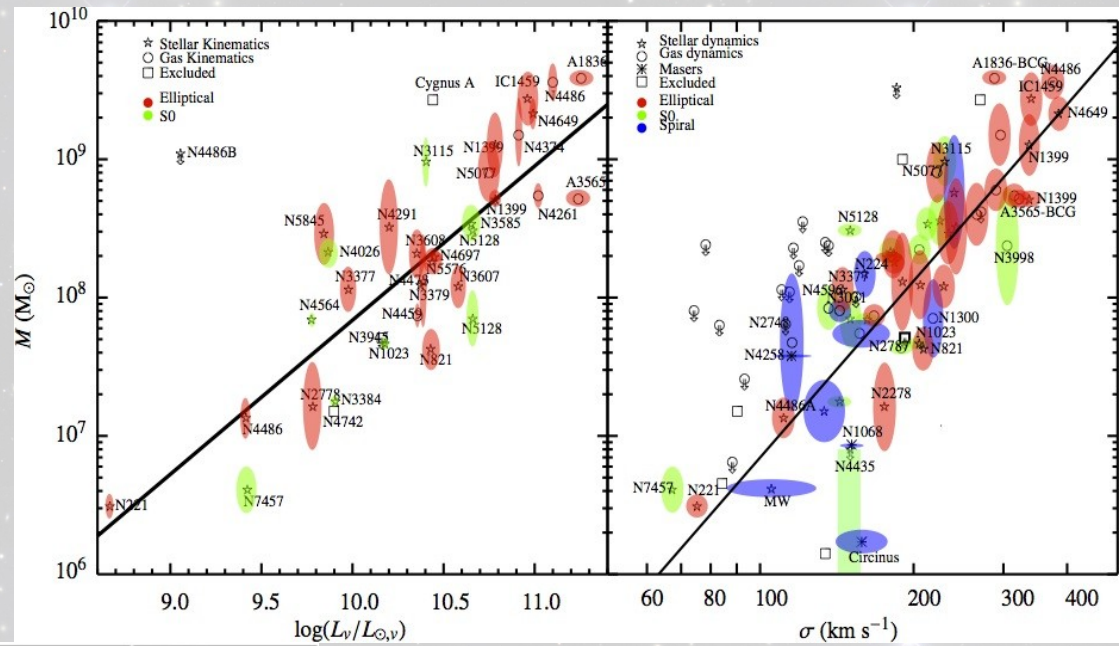
Binary formation

monochromatic

inspiralling

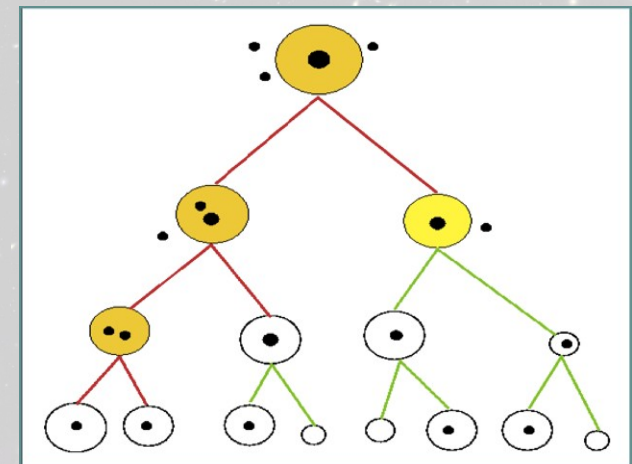
merging/burst

$M_{BH} > 10^7 M_{\odot}$
Distance $z < 2$

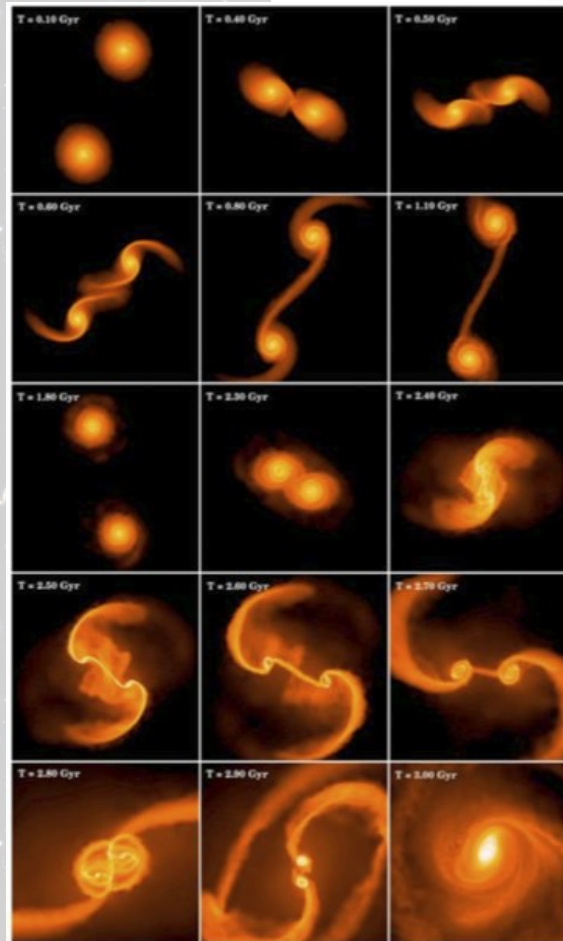


BH vs bulge mass
Gultekin 2009

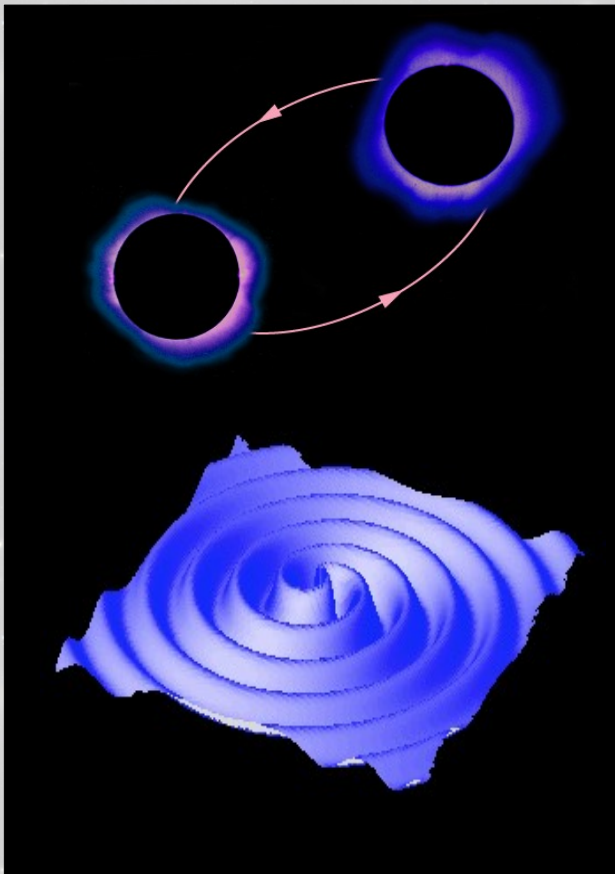
Hierarchical scenario of galaxies formation



Volonteri Haardt Madau 2003

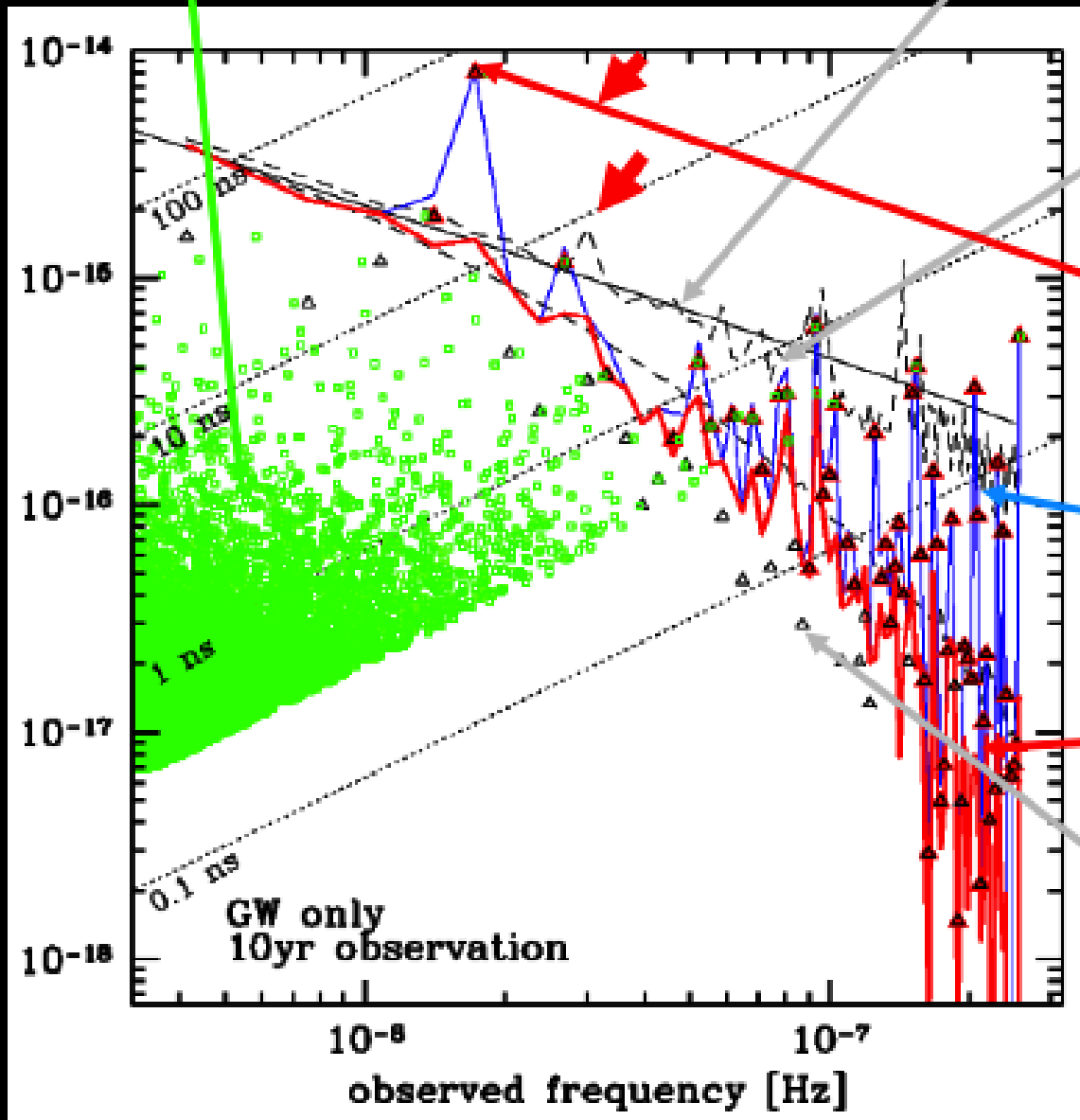


Colpi & Dotti (2009)



SMBBH population : background contribution & single sources

Contribution of individual sources



Theoretical 'average' spectrum

Spectrum averaged over 1000 Monte Carlo realizations

Resolvable systems: i.e. systems whose signal is larger than the sum of all the other signals falling in their frequency bin

Total signal

Unresolved background

Brightest sources in each frequency bin

Pessimistic Scenarii

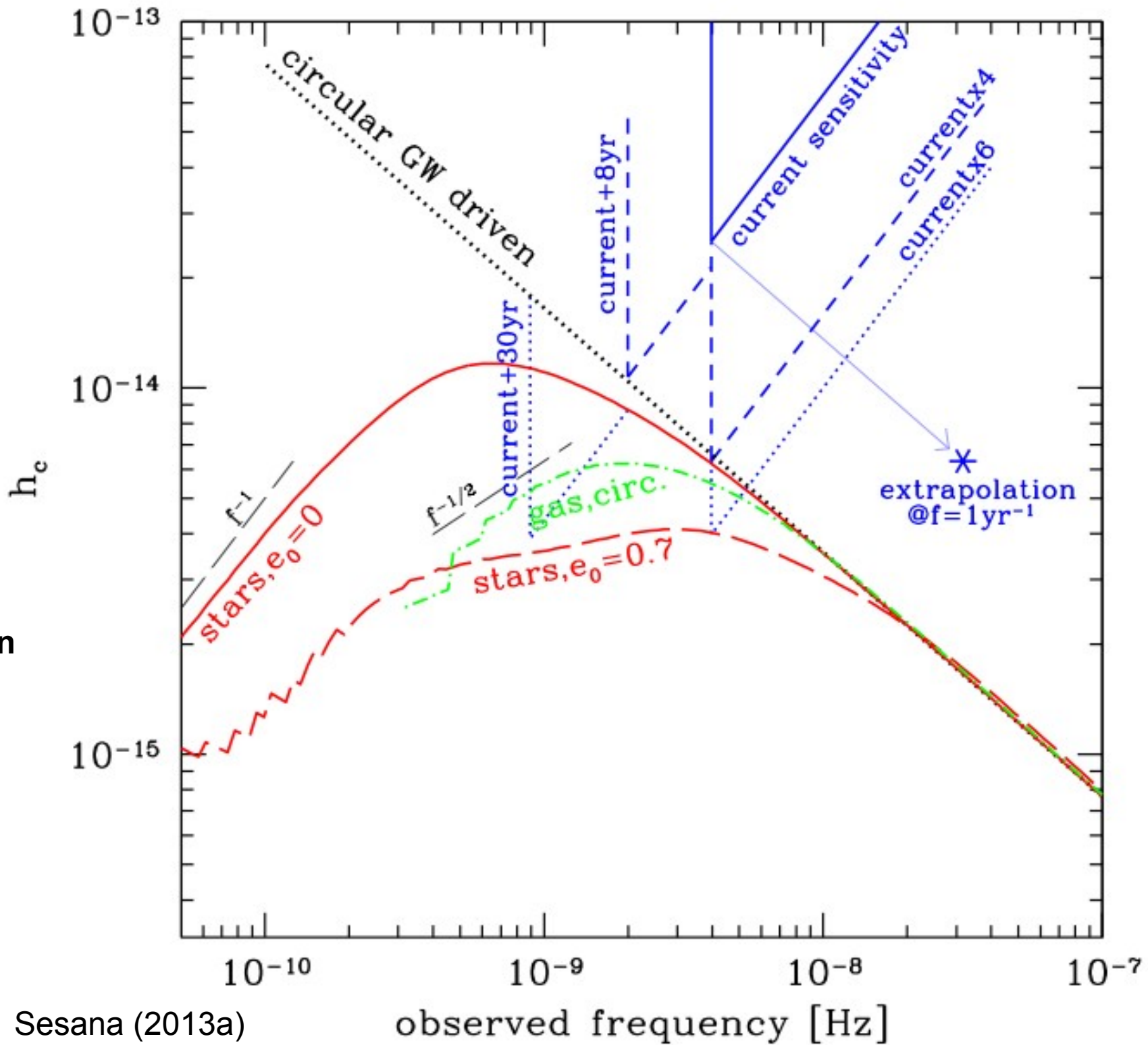
Contribution of accretion discs

+

Spin orientation

Excentricity

Which evolution time scales ?



Earth term & pulsar term

- n : direction of the pulsar
- L : distance Earth – pulsar
- k : direction of the GW propagation
- h_{ij} : GW strain

$$r(t) = \int_0^t \frac{\delta\nu}{\nu}(t') dt'$$

$$\frac{\delta\nu}{\nu}(t) = \frac{1}{2} \frac{\hat{n}^i \hat{n}^j}{1 + \hat{n} \cdot \hat{k}} \left(\underbrace{h_{ij}(t - L(1 + \hat{k} \cdot \hat{n}))}_{\text{Strain of GW at the pulsar}} - \underbrace{h_{ij}(t)}_{\text{Strain of GW at the Earth}} \right)$$

Strain of GW at the pulsar

Strain of GW at the Earth

$$\underline{r_\alpha^e}(t) = \frac{\mathcal{A}}{2\pi f} \left\{ (1 + \cos^2 \iota) F_\alpha^+ [\sin(\omega t + \Phi_0) - \sin \Phi_0] + 2 \cos \iota F_\alpha^\times [\cos(\omega t + \Phi_0) - \cos \Phi_0] \right\},$$

$$\underline{r_\alpha^p}(t) = \frac{\mathcal{A}_\alpha}{2\pi f_\alpha} \left\{ (1 + \cos^2 \iota) F_\alpha^+ [\sin(\omega_\alpha t + \Psi_\alpha + \Phi_0) - \sin(\Psi_\alpha + \Phi_0)] + 2 \cos \iota F_\alpha^\times [\cos(\omega_\alpha t + \Psi_\alpha + \Phi_0) - \cos(\Psi_\alpha + \Phi_0)] \right\},$$

$$F_\alpha^+ = \frac{1}{2} \frac{(\hat{n}^\alpha \cdot \vec{p})^2 - (\hat{n}^\alpha \cdot \vec{q})^2}{1 + \hat{n}^\alpha \cdot \hat{k}}$$

$$F_\alpha^\times = \frac{(\hat{n}^\alpha \cdot \vec{p})(\hat{n}^\alpha \cdot \vec{q})}{1 + \hat{n}^\alpha \cdot \hat{k}}$$

→ 4 x 2 x Nobs x Npsr + 2 x Npsr x NGW

(Matrices 30,000 x 30,000)

Noise analysis

White noise

EFAC, EQUAD

Red noise

Dispersion measure variations

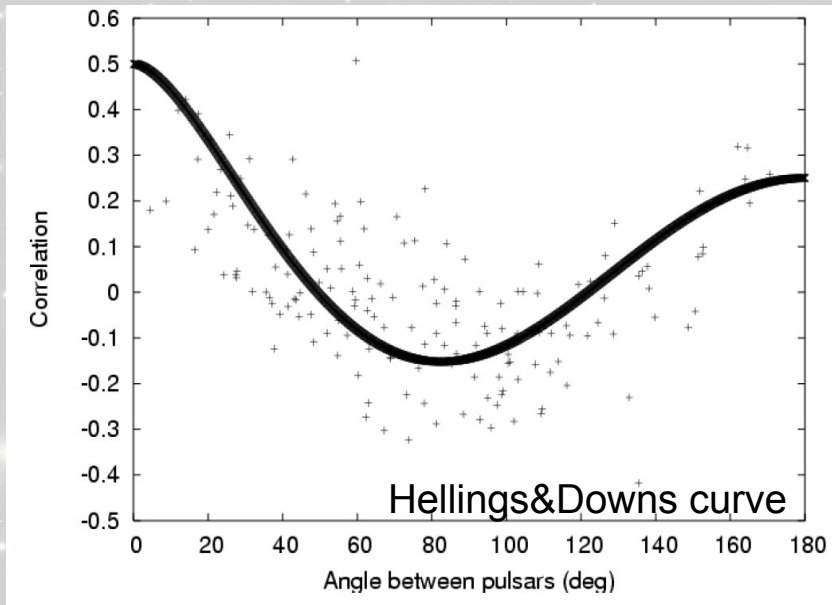
Pulse jitter, timing noise

Clock variations

Solar System ephemerides errors

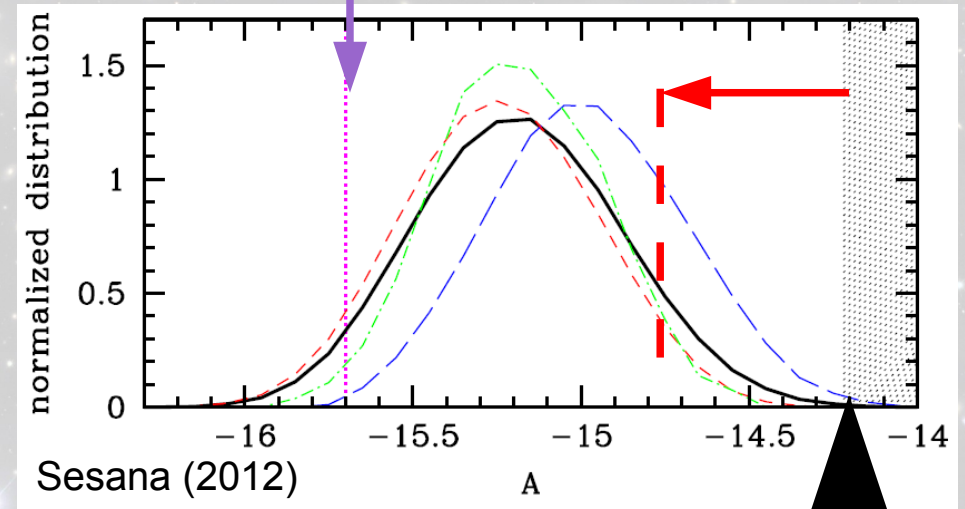
LSR

Gravitational Wave signature

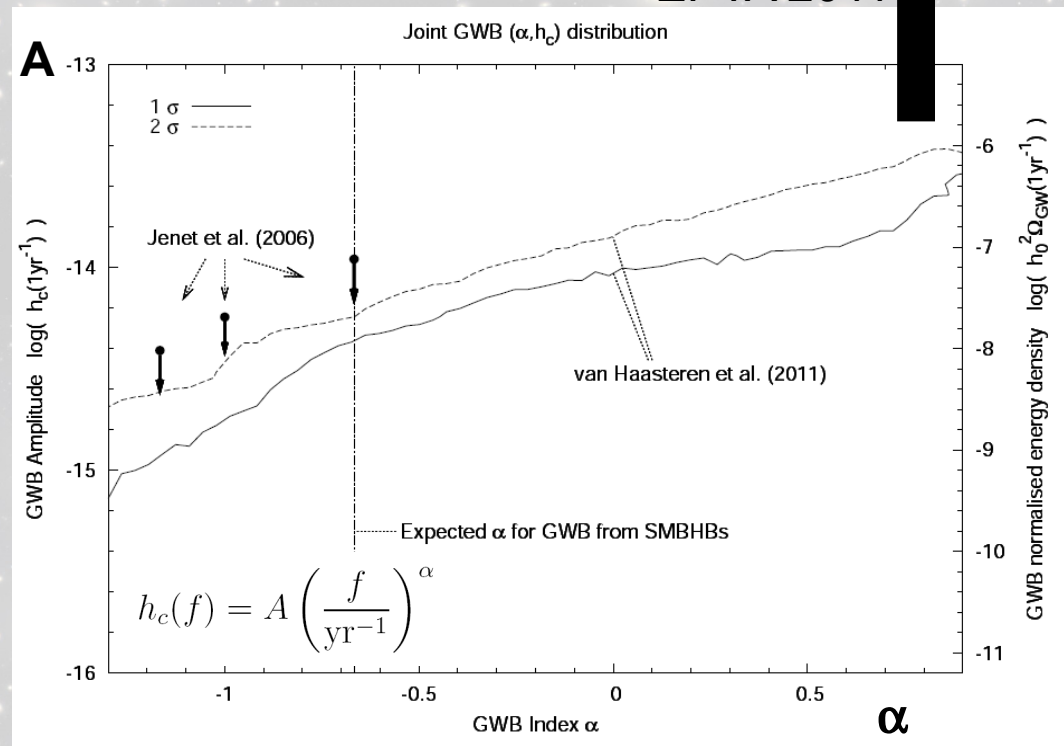


Ideal sample
20 pulsars @ 100 ns

42 pulsars
EPTA 2014 ?



5 pulsars
EPTA 2011



Van Haasteren et al (2011)

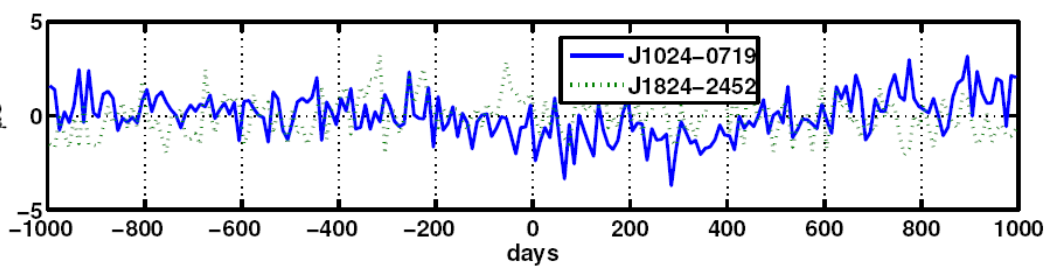
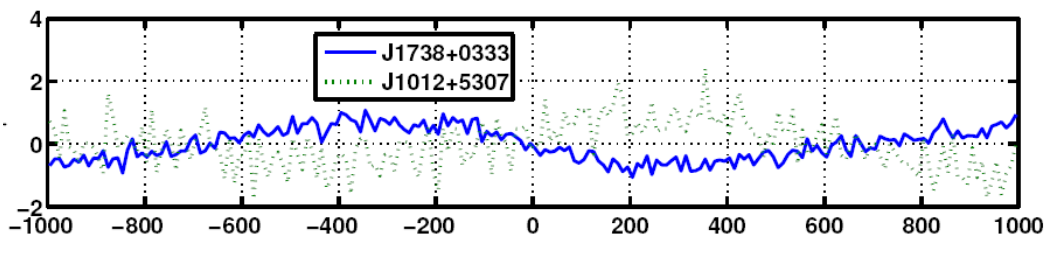
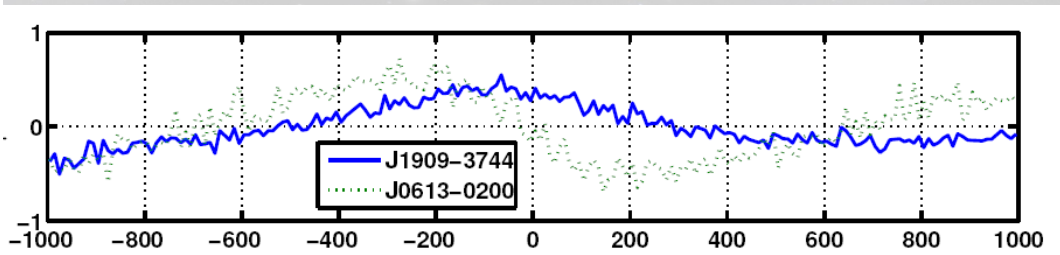
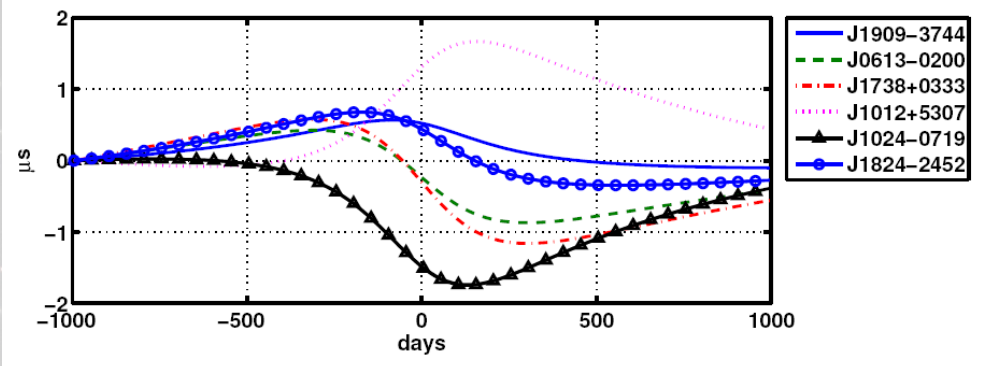
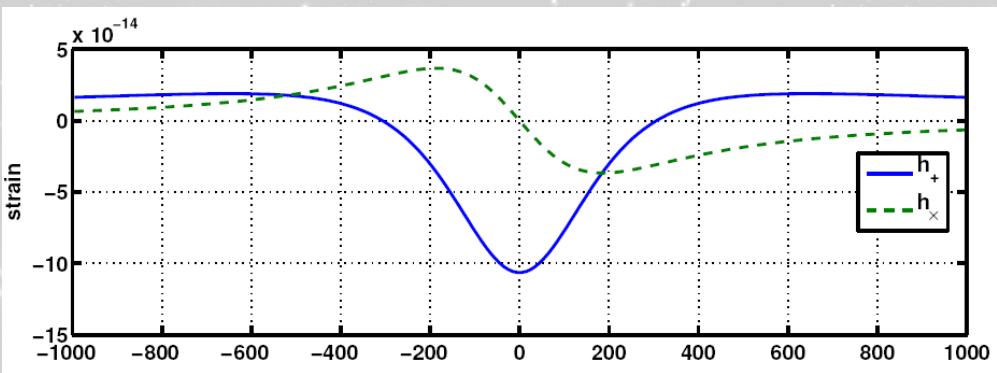
Single source search

Effect of a « burst » at the Virgo Cluster distance (15 Mpc)

Parabolic encounter of two MBH of mass $10^9 M_{\odot}$,

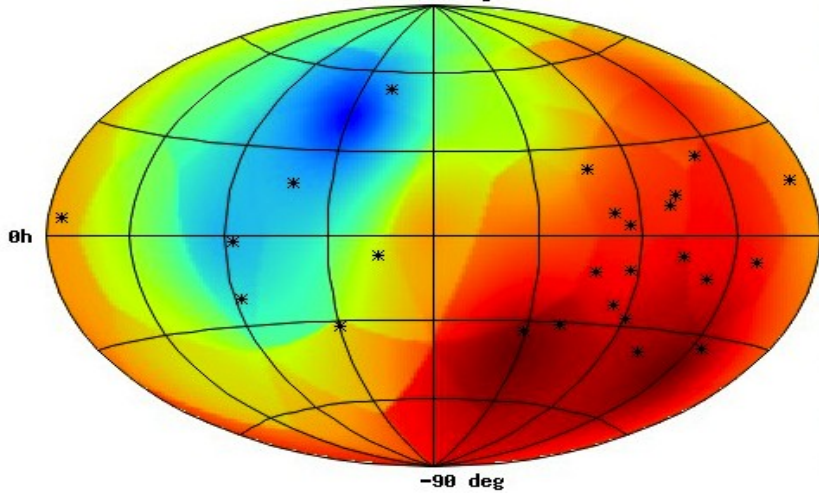
With a impact parameter of 0.02 pc

(Finn & Lommen 2010)



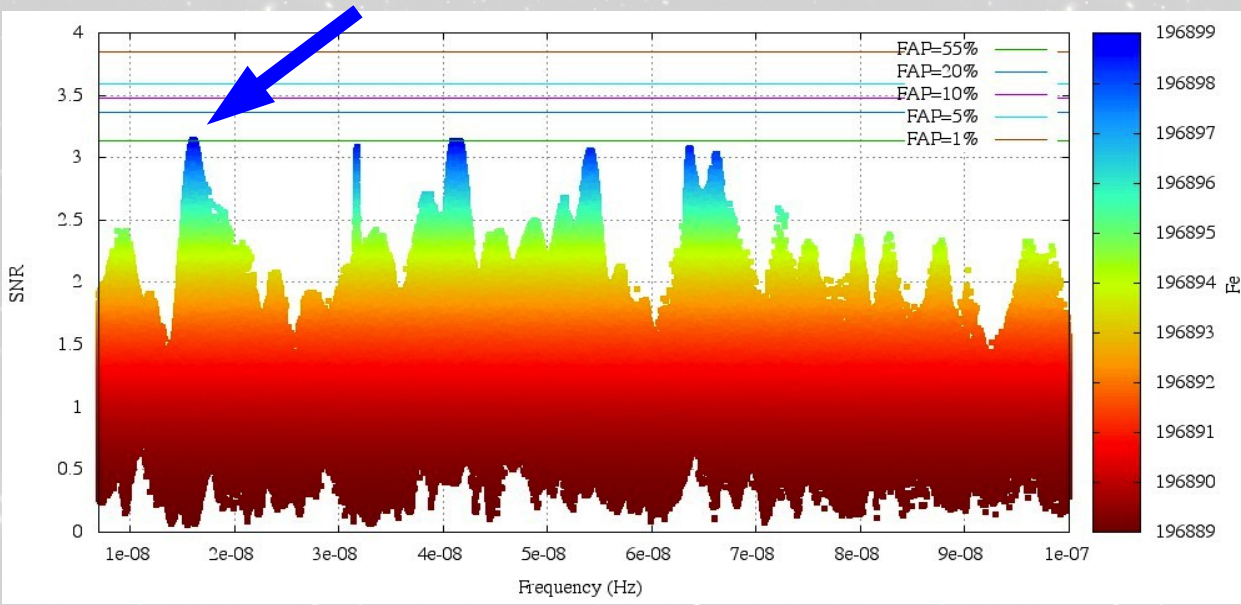
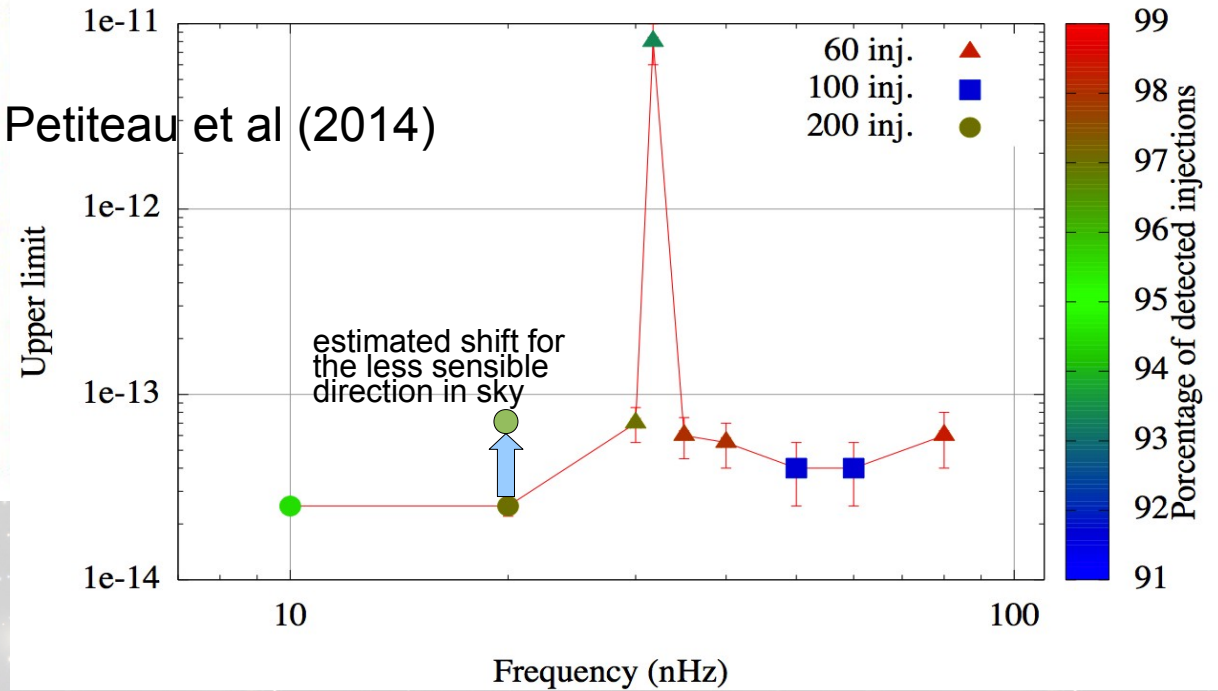
Single source search

20.0 nHz : $\log_{10}(A_{\text{limit}})$



Upper limit : 23 EPTA pulsars

Petiteau et al (2014)



Petiteau et al (2014)

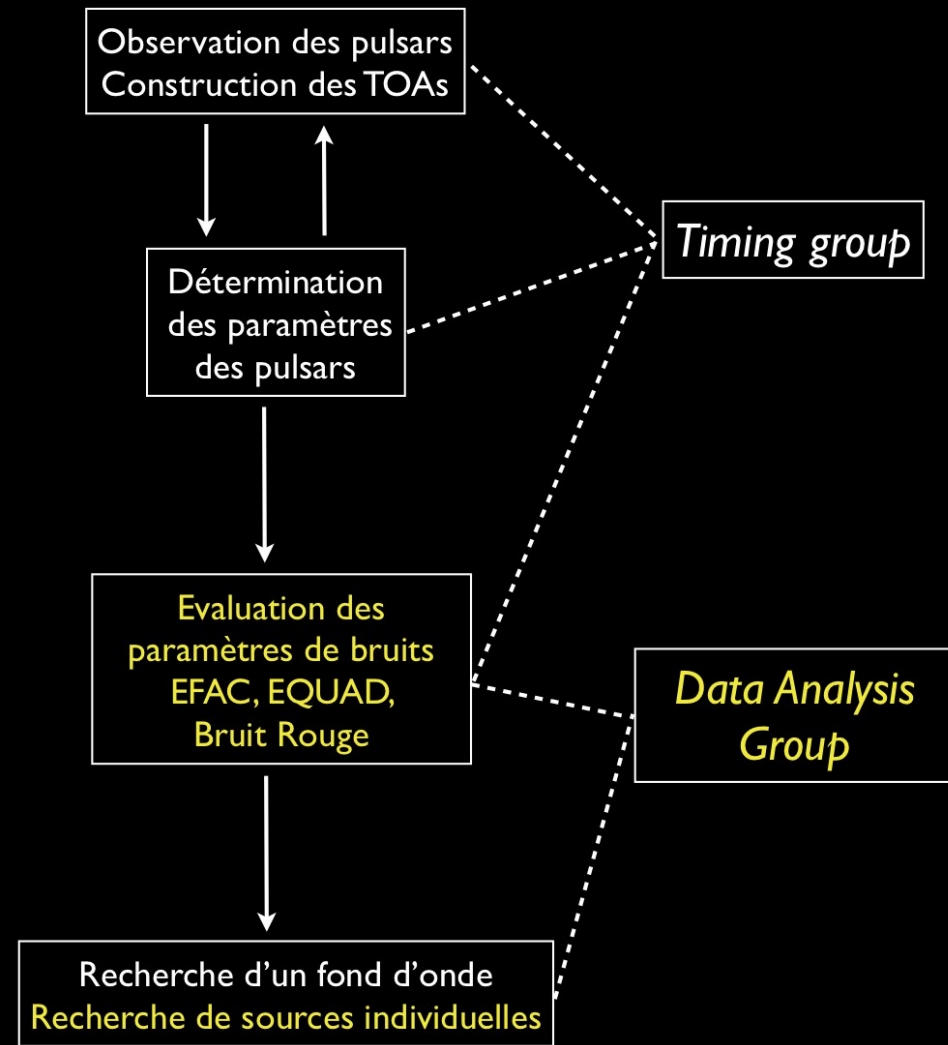
Detection algorithm

Data : 41 EPTA pulsars
(release 09/2013 : preliminary)

Estimator :
Fstatistic, Earth with term only

Best candidate : SNR=3.14
False Alarm Probability=55%

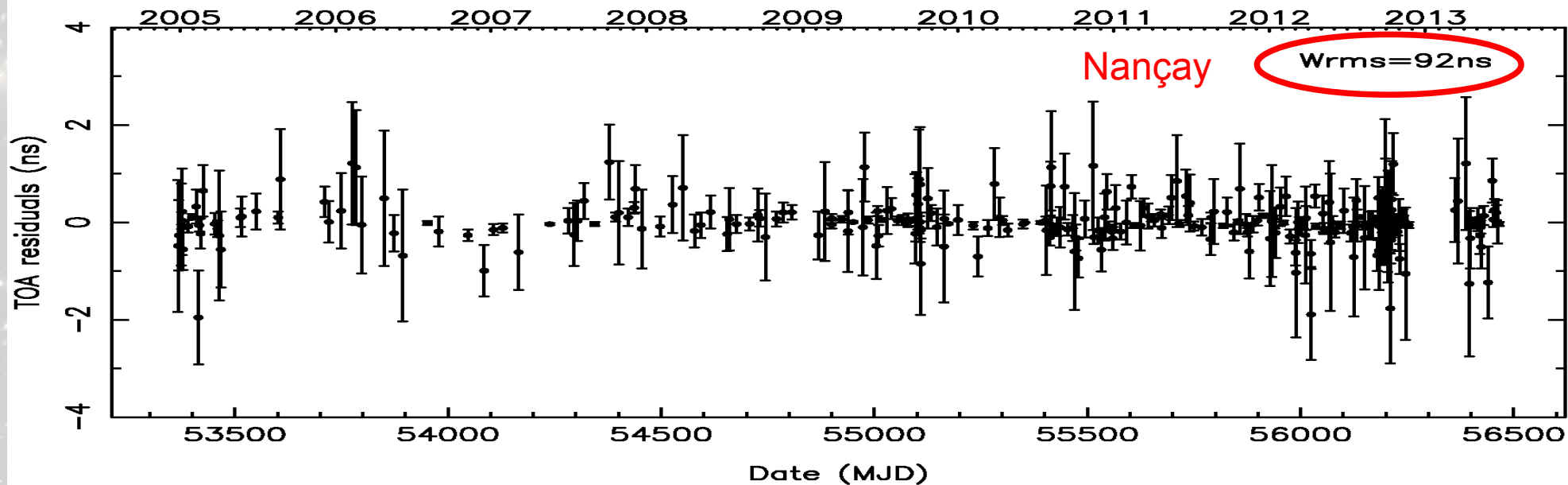
The European Pulsar Timing Array



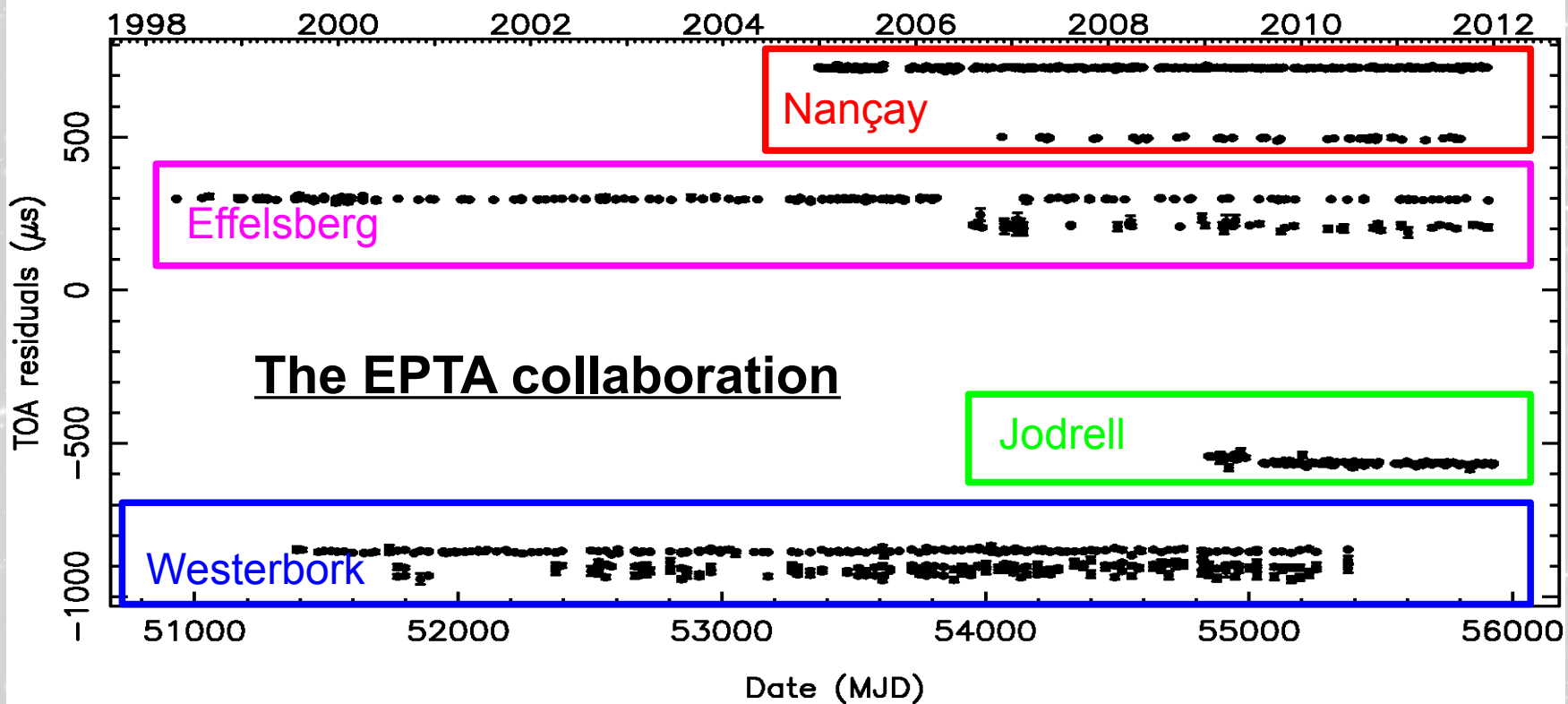
Cf thèse A.Lassus (2013)

Desvignes et al 2014

J1909-3744_NRT



J0613-0200



TOA's

42 pulsars

Span 5-19 years

28 under 5 μ s

4 under 1 μ s
(15 with NUPPI
since 2,5 years)



EPTA, mai 2014 (Dwingeloo) :

**K.Liu, G.Theureau, A.Petiteau, I.Cognard, L.Guillemot, A.Lassus
+ G.Desvignes + PhD 2014 + ANR PTA-France ???**